

Faces of the Order Polytope $\mathcal{O}(E)$ are in bijection with the (closed) E-connected, E-compatible partitions (in blue)